# Numerical Investigation of Tunnel Face Stability Using Forepoling or Fiberglass Nails 

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#### Abstract

Pre-support of tunnel excavation faces using fiberglass nails or forepoling umbrellas aims to improve face stability in cases where an unsupported excavation face will develop uncontrollably large face extrusion, leading to face instability. The paper presents the results of a large set of parametric 3D numerical analyses of tunnel face excavation by the Finite Element Code Simulia Abaqus, using various degrees of reinforcement by fiberglass nails or forepoling umbrellas. The analyses use the average face extrusion as a measure of face stability, considering that face instability is associated with large face extrusions while the safety factor against face instability can be correlated with lower face extrusions in case of pre-supported tunnel faces. The results of the analyses are normalized and a set of semi-empirical formulae and design graphs are produced to calculate the safety factor of supported tunnel faces against instability and other useful quantities in tunnel design (average face extrusion, volume loss and deconfinement coefficient) as a function of ground strength, overburden depth and amount of face reinforcement. The analyses show that tunnel face reinforcement with


[^0]FG nails is much more effective and less costly in securing face stability than the use of forepoling umbrellas. It is shown that even a coarse grid of FG nails can achieve better results than very heavy forepoling, and the difference in effectiveness is more pronounced in weaker ground and or deeper tunnels.

Keywords Tunnelling • Rockmechanics • Soilmechanics • Tunnel face stability • Forepoling umbrella • Fiberglass nailis

## List of Symbols

A Tunnel section area $\left(\mathrm{m}^{2}\right)$
c Soil cohesion (Mohr-Coulomb failure criterion)
D Tunnel width (m)
E Young modulus of the soil or rockmass
$\mathrm{E}_{\mathrm{i}} \quad$ Intact rock Young modulus
GSI Geomechanics Strength Index
H Overburden depth measured from the tunnel axis up to the ground surface
L Length of the tunnel core
$m_{b}, s$, Parameters of the Hoek-Brown failure a criterion
po Average overburden pressure at the tunnel axis (average of vertical and horizontal geostatic stresses).
SF Safety factor of the tunnel face against instability
$\mathrm{U}_{\mathrm{h}} \quad$ Average face extrusion
$\mathrm{U}_{\mathrm{R}} \quad$ Radial convergence of the tunnel wall
V Volume of the core, ahead of the tunnel face
VL Volume loss $=\Delta \mathrm{V} / \mathrm{V}$
$\mathrm{K}_{\mathrm{o}} \quad$ Horizontal geostatic stress coefficient
$\Delta \mathrm{V} \quad$ Reduction of V , due to tunnel wall convergence
$\alpha \quad$ Forepoling stiffness parameter
$\beta \quad$ Fiber-Glass nail density parameter
$\Lambda_{f} \quad$ Face stability parameter
$\lambda \quad$ Deconfinement ratio
$\mathrm{v} \quad$ Poisson ratio of the ground
$\sigma_{\mathrm{ci}} \quad$ Intact rock strength
$\sigma_{\mathrm{cm}} \quad$ Ground strength (for soils and rockmasses)
$\phi \quad$ Soil friction angle (Mohr-Coulomb failure criterion)
$\Omega_{\mathrm{f}} \quad$ Face extrusion parameter

## 1 Introduction

Controlling face stability is very important in tunnelling, as cases of face instability are frequent, severely affect the cost and construction schedule of tunnels and can damage surface structures and utilities in shallow urban tunnels. In mechanized tunnelling with active face pressure (e.g. EPB and Slurry TBMs), the risk of face instability is controlled by the applied face pressure, which is usually adjusted empirically using past performance in "similar" conditions. In tunnelling with conventional techniques (SCL/ NATM), face stability is also assessed empirically in most cases, by subjective comparison of the excavation face with past behaviour of faces under "similar" conditions (i.e., avoiding past failures), occasionally by simplified limit equilibrium analyses (e.g. Leca and Dormieux 1990; Anagnostou and Kovári 1996; Kim and Tonon 2010), and rarely by numerical analysis or systematic measurements of axial face movements (face extrusion). When the risk of face instability is considered unacceptable in SCL/NATM tunnels, the size of the excavation face is reduced or active face support measures are applied, such as fiber-glass (FG) nailing, forepoling, or even leaving a ground wedge on the face. In practically all cases, the capacity of these measures is selected empirically: standard size forepoles $(114 / 100 \mathrm{~mm}$ spaced at 0.50 m over a

120-degree crown arch) or FG nails at a "reasonable" spacing (one anchor per $2.5-5 \mathrm{~m}^{2}$ of face area).

Forepoling umbrellas (FPU) include a set of stiff steel pipes installed ahead of the tunnel face, at the perimeter of the crown of the tunnel. The forepoles are 12 m long steel tubes of diameter $60-170 \mathrm{~mm}$, installed with a typical spacing $S=40-60 \mathrm{~cm}$, at a slight inclination ( 5 to 7 degrees) with respect to the tunnel axis, and cover the upper part of the tunnel wall, at an angle of about 120 degrees. The steel pipes need to overlap along a length of $3-5 \mathrm{~m}$ in order to provide continuous face support as the tunnel face advances. The vertical load from the ground above the forepoles is carried by bending of the forepoles and is transferred to their rear support (steel sets of the temporary lining) and front end support (fixation in the ground ahead of the extruding face core), thus reducing the vertical pressure on the extruding core ahead of the tunnel face. The reduction of the ground load on the extruding core reduces face extrusion and radial wall convergence, thus improving face stability. The reduction of tunnel wall convergence by means of forepoling umbrellas has been studied by several researchers, using 2D and 3D numerical analyses (e.g. Oke et al. 2016).

Fiberglass nails (FGN) have also been used for the reinforcement of tunnel faces. FGN are inserted in holes drilled on the tunnel face at a regular grid, which are then fully cement grouted to ensure full bonding of the nails with the surrounding ground. Their length must be sufficient to permit anchoring beyond the extruding core ahead of the tunnel face. As FG nails are installed in regular distances as the tunnel face advances, a length overlap is crucial in controlling their effectiveness. FGN provide an equivalent pressure on the tunnel face equal to their total tensile force over the face area. Tension of the FGN develops by the tendency of the tunnel face to extrude; thus the FGN reduce face extrusion and radial wall convergence, improving face stability. Peila (1994) reports that use of fiberglass nails can reduce tunnel face deformations by up to $40 \%$. Yoo (2002) based on 3D numerical analyses reports that the use of fiberglass nails can reduce tunnel face deformations by up to $70 \% . \mathrm{Ng}$ and Lee (2002), based on 3D numerical analyses, also highlight the importance of face reinforcement by fiberglass nails in reducing tunnel face deformation and settlements at ground surface.

The effectiveness of various face support measures in improving tunnel face stability has been studied by several researchers, such as: Lunardi and Bindi 2000; Kamata and Mashimo 2003; Anagnostou and Serafeimidis 2007; Kavvadas and Prountzopoulos 2009; Juneja et al. 2010; Dias 2011; Anagnostou and Perazzelli 2015 and Perazzelli and Anagnostou 2020. Despite these efforts, the design of face support measures still remains largely empirical. The main reason of the extensive empiricism in assessing face stability, is that quantitative assessment of face stability requires the definition of a suitable "safety factor", and its calculation using complex threedimensional (3D) numerical analyses with realistic constitutive models and suitably measured/estimated ground parameters. Although seemingly trivial, even the definition of a "safety factor" for face stability analyses is not always straight forward, let alone its numerical calculation. Georgiou et al (2021) have investigated face stability in tunnels with unsupported faces by performing a large set of parametric 3D finite element analyses of the excavation face. In this investigation, the "safety factor" against face instability was defined and calculated in various ground and tunnel conditions.

The present study extends the methods developed by Georgiou et al (2021), to include tunnel faces supported with forepoling umbrellas (FPU) and fiberglass nails (FGN). The investigation method is similar to that used for unsupported tunnel faces: a large set of parametric 3D finite element analyses of the excavation face is performed using the Finite Element Code Simulia Abaqus. In each case of ground conditions and overburden depth, a number of analyses are performed using various densities of FGN reinforcement or forepoling umbrellas to calculate the average face extrusion, which is obviously lower than that of the corresponding unsupported face. The results of the analyses are normalized and a set of semi-empirical formulae are produced to calculate the safety factor of the supported excavation face against instability and other useful quantities in tunnel design (average face extrusion, volume loss and deconfinement coefficient). As these assessments are based and extend on quantities defined in the paper by Georgiou et al (2021) for unsupported tunnel faces, a summary of these findings is given in the next section.

## 2 Face Stability in Tunnels with Unsupported Face

Georgiou et al (2021) investigated face stability in tunnels with unsupported faces by performing 1203 D finite element analyses of the excavation face with the Finite Element Code Simulia Abaqus, varying ground conditions (in soils and weak rockmasses) and overburden depths. The analyses calculate the axial displacement (face extrusion) at all integration points on the tunnel face. These values are averaged over the tunnel face to give an "average face extrusion" $\left(\mathrm{U}_{\mathrm{h}}\right)$ which is then normalized by the tunnel width (D) and a modulus-to-depth factor $\left(\mathrm{E} / \mathrm{p}_{\mathrm{o}}\right)$ to give the dimensionless "face extrusion parameter" $\left(\Omega_{f}\right)$ :
$\Omega_{f}=\left(\frac{U_{h}}{D}\right)\left(\frac{E}{p_{o}}\right)$
where $E$ is the elastic Young modulus of the ground (soil or rockmass) and $p_{\mathrm{o}}=0.5\left(1+\mathrm{K}_{\mathrm{o}}\right) \gamma \mathrm{H}$ is the average overburden pressure at the tunnel axis (average of vertical and horizontal geostatic stresses).

The 120 values of the calculated face extrusion parameter $\left(\Omega_{f}\right)$ were then plotted against various forms of strength-to-stress ratio, in search of an optimal correlation. The optimal correlation was achieved for the following dimensionless "face stability parameter" $\left(\Lambda_{f}\right)$ :
$\Lambda_{f}=3.8\left(\frac{\sigma_{c m}}{\gamma H \sqrt{1+(2 / 3) K_{o}}}\right)\left(\frac{H}{D}\right)^{0.35}$
which combines ground strength ( $\sigma_{\mathrm{cm}}$ ), average overburden stress ( $\mathrm{p}_{\mathrm{o}}$ ) and tunnel width ( D ). Georgiou et al. (2021) have shown that this parameter can best describe the relevant parameters of the tunnel excavation face (face extrusion, volume loss, radial wall displacement, deconfinement ratio and safety factor against stability), in the sense that the calculated values in the FE analyses correlate well with the corresponding parameter $\left(\Lambda_{f}\right)$. Control analyses have shown that the above formula can also be used in various tunnel shapes, including separate excavation of the top heading of a tunnel, via an equivalent tunnel size parameter $D=1.15 \operatorname{sqrt}(\mathrm{~A})$, where A is the section area of the tunnel or phase.

In soils, the ground strength was calculated by the Uniaxial Compressive Strength using the MohrCoulomb failure criterion:

$$
\begin{equation*}
\sigma_{c m}=2 c \tan \left(45^{\circ}+\varphi / 2\right) \tag{3a}
\end{equation*}
$$

In weak or very fractured rockmasses, yielding was modelled by the Hoek-Brown failure criterion. In this case, "rockmass strength" $\left(\sigma_{\mathrm{cm}}\right)$ and "rockmass modulus" (E) were calculated by the following empirical formulae, in terms of the Geological Strength Index—GSI (Hoek and Diederichs 2006; Litsas et al 2017):
$\sigma_{c m}=0.02 \sigma_{c i} \exp \left(\frac{G S I}{25.5}\right)$
$E=E_{i}\left[0.02+\frac{1}{1+\exp [(60-G S I) / 11]}\right]$
In an unsupported tunnel face, the optimal correlation between face extrusion $\left(\Omega_{\mathrm{f}}\right)$ and face stability parameter $\left(\Lambda_{f}\right)$ is given by the formula:
$\Omega_{f}=1.4 \Lambda_{f}^{-1.2}$
This formula can be used to estimate the face extrusion parameter $\left(\Omega_{f}\right)$ and, via Eq. 1, calculate the average face extrusion $\left(\mathrm{U}_{\mathrm{h}}\right)$ for an unsupported tunnel face with given $\left(\Lambda_{f}\right)$, i.e., a tunnel of size (D), overburden depth $(\mathrm{H})$, in ground with strength ( $\sigma_{\mathrm{cm}}$ ).

The above correlation shows that, when $\Lambda_{f}<1$, the face extrusion parameter $\left(\Omega_{\mathrm{f}}\right)$ starts to increase rapidly, with values $\Omega_{\mathrm{f}}>1.4$. Thus, the condition $\left(\Lambda_{f}\right)_{\text {lim }}=1$, corresponding to face extrusion $\left(\Omega_{\mathrm{f}}\right)_{\text {lim- }}$ $=1.4$, was considered as limiting face stability in unsupported tunnel faces.

At limiting face stability, Eqs. (4), (1) and (2) give the limiting face extrusion and limiting ground strength in unsupported tunnel faces:
$\left(\Omega_{f}\right)_{\lim }=1.4 \Rightarrow\left(\frac{U_{h}}{D}\right)_{\lim }=1.4\left(\frac{p_{o}}{E}\right)$
$\left(\sigma_{c m}\right)_{\lim }=0.263 \gamma H \sqrt{1+(2 / 3) K_{o}}\left(\frac{D}{H}\right)^{0.35}$
where $\left(\sigma_{\mathrm{cm}}\right)_{\text {lim }}$ is the lowest ground strength to ensure limiting stability of an unsupported face for a tunnel with width (D) and overburden depth (H).

Since stable tunnel faces correspond to $\Lambda_{f}>1$ and unstable faces to $\Lambda_{f}<1$, the safety factor (SF) of a tunnel face (either unsupported or supported) can be defined by the ratio of the face stability parameter $\left(\Lambda_{f}\right)$, defined by Eq. (2) and depending only on tunnel
geometry and ground strength, to the corresponding limiting value $\left(\Lambda_{f}\right)_{\lim }$ (corresponding to face extrusion $\left(\Omega_{\mathrm{f}}\right)_{\lim }=1.4$ for any tunnel face $)$ :
$S F=\frac{\Lambda_{f}}{\left(\Lambda_{f}\right)_{\lim }}$
For an unsupported tunnel face, $\left(\Lambda_{f}\right)_{\text {lim }}=1$ and thus (using Eqs. 6 and 2):
$S F_{o}=3.8\left(\frac{\sigma_{c m}}{\gamma H \sqrt{1+(2 / 3) K_{o}}}\right)\left(\frac{H}{D}\right)^{0.35}$
For supported tunnel faces, $\left(\Lambda_{f}\right)_{\text {lim }}<1$, due to the beneficial effect of the face support measures. Thus, the reduction of the limiting face stability parameter by the face support measures, increases the safety factor of an initially unstable unsupported tunnel face ( $\Lambda_{f}<1$ ), possibly rendering the tunnel face stable (if SF $>1$ ). The present paper calculates the decrease of the limiting face stability parameter by the face support measures, and thus calculates the safety factor of supported tunnel faces (from Eq. 6).

For unsupported tunnel faces, the face stability parameter $\left(\Lambda_{f}\right)$ is also used to calculate the radial displacement $\left(\mathrm{U}_{\mathrm{R}}\right)$ of the tunnel wall at the excavation face:
$\frac{U_{R}}{D}=1.75\left(\frac{p_{o}}{E}\right)\left(\Lambda_{f}\right)^{-1.2}$
and the corresponding volume loss (VL), caused by $\left(\mathrm{U}_{\mathrm{R}}\right)$ which "squeezes" the core ahead of the tunnel face, giving face extrusion $\left(\mathrm{U}_{\mathrm{h}}\right)$. Volume loss (VL) is defined as the reduction $(\Delta \mathrm{V})$ of the volume $(\mathrm{V})$ of the extrusion core ahead of the tunnel face per unit volume of the core $(\mathrm{VL}=\Delta \mathrm{V} / \mathrm{V})$ :
$V L=1.83\left(\frac{p_{o}}{E}\right)\left(\Lambda_{f}\right)^{-1.2}$
Finally, the face stability parameter $\left(\Lambda_{f}\right)$ is used to calculate the deconfinement ratio $(\lambda)$ at the tunnel face by the formula:
$\lambda=0.25+0.75 \exp \left(-\Lambda_{f} / 2\right)$
At limiting face stability $\left(\Lambda_{f}=1\right)$, the deconfinement ratio at the tunnel face is: $\lambda_{\lim }=0.70$.

In supported tunnel faces, quantities $\left(\mathrm{U}_{\mathrm{R}}\right),(\mathrm{VL})$ and $(\lambda)$ can be calculated by the same formulae, replacing $\left(\Lambda_{f}\right)$ by the corresponding limiting value $\left(\Lambda_{f}\right)_{\text {lim }}$ which depends on the face support measures.

## 3 Numerical Investigation of Supported Tunnel Faces

The present study extends the above methods to include tunnel faces supported with forepoling umbrellas (FPU) and fiber-glass nails (FGN). The investigation method includes a large set of parametric 3D finite element analyses of the excavation face, using the Finite Element Code Simulia Abaqus. Figure 1 shows the shape of the tunnel section used in the analyses.

Figure 2 shows the finite element mesh used in the analyses, with eight-node hexahedral finite elements. Due to symmetry about the vertical plane, only the left half of the model is analysed. Following a sensitivity analysis, the extent of the finite element mesh is sufficiently large (at least 3.5 D in each direction) to minimize boundary effects in all directions. The conditions on the tunnel face are assessed after an initial tunnel advance by 5 to 7 D from the left (start) edge of the FE mesh, leaving a clear distance 3.5 to 5.5 D from the right end boundary (ahead of the tunnel face). For overburden depths $\mathrm{H}>3 \mathrm{D}$, additional overburden is simulated as a surface pressure, because ground stiffness and strength in this zone does not influence tunnel excavation. The tunnel section is excavated in a single phase (full face excavation) with excavation steps of 1 m (equal to the size of the elements in the axial direction). In each excavation step, a relatively stiff ( 30 cm thick) shotcrete liner is installed on the tunnel wall (full ring) 2 m behind the excavation face. The shotcrete liner is modelled as linearly elastic 4-noded shell elements, with a relatively low concrete modulus equal to $\mathrm{E}=15 \mathrm{GPa}$ to


Fig. 1 Cross-section of the oval-shaped tunnel used in the finite element analyses. Width $\mathrm{D}=10 \mathrm{~m}$, section area $\mathrm{A}=67.3 \mathrm{~m}^{2}$
account for concrete setting time during tunnel advance. Parametric analyses have shown that the thickness and stiffness of the shotcrete shell do not influence the magnitude of face extrusion (which is of main interest in the present study).

Forepoling tubes are modelled as horizontal beams spanning the tunnel crown at an angle 120 degrees ( 60 degrees at each side of the crown) with spacing $\mathrm{S}=0.50 \mathrm{~m}$. The beams are very long, to avoid the need to install new forepoles every several meters of tunnel advance. Parametric analyses have shown that the replacement of the slightly inclined forepoles with horizontal beams does not influence the accuracy of the results. The beams are modelled as elasticperfectly plastic with elastic modulus $\mathrm{E}=200 \mathrm{GPa}$, Poisson ratio $v=0.25$ and yield stress 235 MPa . The following six types of forepoling beams are used in the analysis (the lighter tubes aimed to confirm that the numerical solution converges to the unsupported face condition when the forepoling stiffness tends to zero):

The moment of inertia (I) per meter width was calculated for forepole spacing $S=0.50 \mathrm{~m}$ as:
$I=\frac{\pi}{64 S}\left(d_{o}^{4}-d_{i}^{4}\right) \quad$ in $\mathrm{mm}^{4} / \mathrm{mm}$
Table 1 also shows the corresponding values of a forepoling stiffness parameter ( $\alpha$ ), defined as:
$\alpha=0.05 I^{0.125} \quad$ in $(\mathrm{mm})^{3 / 8}$
Fiberglass nails are modelled as horizontal truss elements, evenly spaced on the tunnel face. The nails are very long, to avoid the need to install new nails every several meters of tunnel advance. The nails are modelled as elastic-perfectly plastic with elastic modulus $\mathrm{E}=40 \mathrm{GPa}$, Poisson ratio $v=0.30$, yield load $\mathrm{P}_{\mathrm{u}, \mathrm{FG}}=200 \mathrm{kN}$ and mobilisation factor $50 \%$ of the yield load ( $\mathrm{F}=2$ ). Three nail densities ( $\mathrm{n} / \mathrm{A}$ ) are examined: one anchor per $1.0,2.0$ and $4.0 \mathrm{~m}^{2}$ of tunnel face area. For each anchor density, the following dimensionless FGN density parameter ( $\beta$ ) is defined:
$\beta=1.2\left(\frac{n P_{u, F G}}{F A p_{a}}\right)^{0.35}$
where ( n ) is the number of FG nails on tunnel face (A), $\mathrm{P}_{\mathrm{u}, \mathrm{FG}}=200 \mathrm{kN}$ is the yield load of the nails, $\mathrm{F}=2$ is the nail force mobilisation factor (FE analyses show that FG nails develop tension equal to about $50 \%$ of the yield strength) and $p_{a}$ is the atmospheric pressure


Fig. 2 Finite element mesh used in the analyses. The case shown corresponds to overburden depth $\mathrm{H}=3 \mathrm{D}=30 \mathrm{~m}$. The right part of the figure shows the model of the forepoles (horizontal beams) and the fiberglass nails (horizontal truss elements)

Table 1 Forepoling tubes used in the analyses

| Outside diameter <br> do $(\mathrm{mm})$ | Wall thickness <br> $\mathrm{t}(\mathrm{mm})$ | Moment of inertia I <br> $\left(\mathrm{mm}^{4} / \mathrm{m}\right)$ | Forepole stiffness <br> parameter a $\left(\mathrm{mm}^{3 / 8}\right)$ | Section modulus W <br> $\left(\mathrm{cm}^{3} / \mathrm{m}\right)$ | Yield moment My <br> $(\mathrm{kNm} / \mathrm{m})$ |
| :--- | :--- | :--- | :--- | :---: | :---: |
| 20 | 1 | 5.40 | 0.062 | 0.54 | 0.13 |
| 25 | 2 | 19.26 | 0.072 | 1.54 | 0.36 |
| 34 | 3 | 70.85 | 0.085 | 4.17 | 0.98 |
| 70 | 7 | 1391.8 | 0.124 | 39.76 | 9.34 |
| 114.3 | 7 | 6820.7 | 0.151 | 119.35 | 28.05 |
| 168.3 | 7 | $23,115.8$ | 0.176 | 274.70 | 64.55 |

$\left(\mathrm{p}_{\mathrm{a}}=100 \mathrm{kPa}\right)$ used for normalisation purposes. The three nail densities examined ( $\mathrm{n} / \mathrm{A}=$ one nail per 1.0, 2.0 and $4.0 \mathrm{~m}^{2}$ of tunnel face area) give density parameters $\beta=1.20,0.94$ and 0.74 , respectively.

The numerical analyses include shallow tunnels in soils and deep tunnels in weak or heavily fractured rockmass. In each ground/overburden combination, a number of analyses are performed using various degrees of reinforcement by fiberglass nails (three nail densities) or forepoling umbrellas (six forepoling types) to calculate the average face extrusion of the supported tunnel face and compare it to the corresponding values of the unsupported face.

Shallow tunnels:
In shallow tunnels, two cases of overburden depth (measured from the tunnel axis up to the ground surface), are examined: $H=20 \mathrm{~m}(\mathrm{H} / \mathrm{D}=2)$ and $\mathrm{H}=30 \mathrm{~m} \quad(\mathrm{H} / \mathrm{D}=3)$, with ground unit weight $\gamma=20 \mathrm{kN} / \mathrm{m}^{3}$ and two cases of the horizontal geostatic stress coefficient: $\mathrm{K}_{\mathrm{o}}=0.5$ and 1.0 (to include the effect of the horizontal stress ratio). The ground is relatively stiff elastic-perfectly plastic,
with elastic modulus (E), Poisson ratio $\mathrm{v}=0.33$, yielding according to the Mohr-Coulomb criterion ( $c=$ cohesion, $\varphi=$ friction angle). The assumption of a linearly elastic-perfectly plastic material is a necessary simplifying assumption for the present parametric analyses, since a more advanced model (such as strain hardening or softening) introduces additional parameters to be investigated, making the

Table 2 Sets of ground parameters used in the analyses of shallow tunnels

| $c(\mathrm{kPa})$ | $\varphi\left({ }^{\circ}\right)$ | $\sigma_{c m}(\mathrm{kPa})$ | $E(\mathrm{MPa})$ |
| :--- | :--- | :---: | :--- |
| 20.0 | 22.5 | 59.9 | 80 |
| 20.0 | 25.0 | 62.8 | 100 |
| 25.0 | 25.0 | 78.5 | 120 |
| 30.0 | 25.0 | 94.2 | 150 |
| 30.0 | 30.0 | 103.9 | 170 |
| 50.0 | 30.0 | 173.2 | 200 |

parameter combinations intractable. Table 2 shows the six sets of ground parameters used in the analyses.

According to the Mohr-Coulomb failure criterion, the ground strength $\left(\sigma_{\mathrm{cm}}\right)$ is equal to the Uniaxial Compressive Strength defined by Eq. (3a). The E-modulus is rather large, because it represents the elastic response before plastic yielding. After yielding, stiffness is drastically reduced by the accumulation of plastic strains. The total number of numerical analyses of shallow tunnels was 24 (two tunnel depths, two $\mathrm{K}_{\mathrm{o}}$ values and six sets of material parameters).

Deep tunnels:
In deep tunnels, three overburden depths are examined: $\mathrm{H}=100 \mathrm{~m}, 150 \mathrm{~m}$ and 200 m in weak or heavily fractures rockmass with unit weight $\gamma=25$ $\mathrm{kN} / \mathrm{m}^{3}$, horizontal geostatic stress coefficient $\mathrm{K}_{\mathrm{o}}=0.5$ and 1.0 (two cases), intact rock properties $\sigma_{\text {ci- }}$ $=10 \mathrm{MPa}$ and $\mathrm{E}_{\mathrm{i}}=2 \mathrm{GPa}$, Poisson ratio $\mathrm{v}=0.33$ and Geological Strength Index in the range GSI $=25$ to 45 (three cases). The rockmass was assumed linearly elastic—perfectly plastic, yielding according to the Generalised Hoek-Brown failure criterion (Hoek et al 2002) with various parameters ( $\left.m_{b}, s, a\right)$. Table 3 shows the three sets of rockmass parameters used in the parametric analyses.

The "rockmass strength" $\left(\sigma_{\mathrm{cm}}\right)$ and "rockmass modulus" (E) for the various GSI values are calculated by formulae (3b). The total number of numerical analyses for the deep tunnels was 18 (three tunnel depths, two $\mathrm{K}_{\mathrm{o}}$ values, and three sets of material parameters).

The total number of numerical analyses with supported face was $(24+18) \times 6=252$ with forepoling and $(24+18) \times 3=126$ with face nailing, plus $(24+18)=42$ cases without face reinforcement.

Each numerical analysis calculates the axial displacement (face extrusion) at all integration points on the tunnel face. These values are averaged over the

Table 3 Sets of rockmass parameters used in the analyses of deep tunnels

| $G S I$ | $m_{b}$ | $s$ | $a$ | $\sigma_{c m}(\mathrm{MPa})$ | $E(\mathrm{MPa})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 25 | 0.687 | $2.4 \times 10^{-4}$ | 0.531 | 0.53 | 119.7 |
| 35 | 0.981 | $7.3 \times 10^{-4}$ | 0.516 | 0.79 | 226.8 |
| 45 | 1.403 | $2.0 \times 10^{-3}$ | 0.508 | 1.17 | 447.3 |

tunnel face to give an "average face extrusion" $\left(\mathrm{U}_{\mathrm{h}}\right)$ which is then normalized by the tunnel width (D) and a modulus-to-depth factor $\left(\mathrm{E} / \mathrm{p}_{\mathrm{o}}\right)$ to give the dimensionless "face extrusion parameter" $\left(\Omega_{\mathrm{f}}\right)$ defined in Eq. (1). The face extrusion parameter of the unsupported tunnel face is denoted as $\left(\Omega_{\mathrm{fo}}\right)$ and the reduction of the face extrusion parameter with respect to the unsupported face is:
$\Delta \Omega_{f}=\Omega_{f o}-\Omega_{f} \rightarrow \frac{\Delta \Omega_{f}}{\Omega_{f o}}=1-\frac{\Omega_{f}}{\Omega_{f o}}$


Fig. 3 a Effect of forepoling stiffness on the reduction of the average face extrusion, plotted versus the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$. $\mathbf{b}$ Effect of forepoling stiffness on the reduction of the average face extrusion, plotted versus the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$. The vertical axis is normalized with an optimally selected forepoling stiffness parameter ( $\alpha$ )

## 4 Analysis of Face Support with Forepoling Umbrellas (FPU)

Figure 3a plots the calculated decrease of the face extrusion parameter ( $\Delta \Omega_{\mathrm{f}}$ ), normalized with the corresponding face extrusion of the unsupported face $\left(\Omega_{\mathrm{fo}}\right)$, versus the face stability parameter $\left(\Lambda_{f}\right)$ (defined by Eq. 2), for tunnel faces supported with six types of forepoles. Stiffer forepoles (with higher moment of inertia I-see Table 1) reduce face extrusion more, while forepoles of very small stiffness give very small extrusion reductions, comparable with the unsupported face ( $\Delta \Omega_{\mathrm{f}}=0$ ), confirming the robustness of the numerical algorithm. Larger values of the face stability parameter $\left(\Lambda_{f}\right)$, corresponding to better ground strength/overburden stress combinations, cause smaller face extrusions for all forepoling types. For $\Lambda_{f}>2$, face extrusion is very small even in unsupported faces ( $\Omega_{\mathrm{fo}}<0.5$ ) and thus the additional decrease of face extrusion due to face reinforcement is negligible for all types of forepoles, rendering the use of face support by forepoling as practically useless.

In Fig. 3b, the vertical axis is normalized with a forepoling stiffness parameter $(\alpha)$, defined by Eq. (12a). Parameter ( $\alpha$ ) was optimally selected to reduce the scatter of the face extrusion reductions $\left(\Delta \Omega_{\mathrm{f}}\right)$ shown in Fig. 3a for the commonly used forepoles ( $\mathrm{d}_{\mathrm{o}}>70 \mathrm{~mm}$ ); most of the data points deviating a lot from the best fit curve correspond to small diameter forepoles, not used in practical applications. The best fit curve in Fig. 3b can be expressed by the formula (combined with Eq. 4):

$$
\begin{equation*}
\left(\frac{1}{\alpha}\right)\left(\frac{\Delta \Omega_{f}}{\Omega_{f o}}\right)=\left(\Lambda_{f}\right)^{-1.7} \Rightarrow \Delta \Omega_{f}=1.4 \alpha\left(\Lambda_{f}\right)^{-2.9} \tag{14a}
\end{equation*}
$$

Using this formula, the face extrusion parameter $\left(\Omega_{\mathrm{f}}\right)$ of the supported tunnel faces can be expressed as:

$$
\begin{align*}
\Omega_{f} & =\Omega_{f o}\left[1-\alpha\left(\Lambda_{f}\right)^{-1.7}\right] \Rightarrow \Omega_{f} \\
& =1.4\left(\Lambda_{f}\right)^{-1.2}\left[1-\alpha\left(\Lambda_{f}\right)^{-1.7}\right] \tag{14b}
\end{align*}
$$

Using Eq. (1), the above formula can be used to calculate the average face extrusion $\left(U_{h}\right)$ for various ground strength/overburden stress combinations and various forepoling stiffnesses (i.e., values of the $\alpha$ parameter):
$\frac{U_{h}}{D}=1.4\left(\frac{p_{o}}{E}\right)\left(\Lambda_{f}\right)^{-1.2}\left[1-\alpha\left(\Lambda_{f}\right)^{-1.7}\right]$
Figure 4 plots the relationship of the face extrusion parameter $\left(\Omega_{f}\right)$ versus ( $\Lambda_{f}$ ), for selected values of forepoling stiffness parameter ( $\alpha$ ), using Eq. (14b). Appreciable reduction of face extrusion occurs for $\Lambda_{\mathrm{f}}<1$, where the unsupported face has limiting stability, with increasing values of the forepoling stiffness parameter ( $\alpha$ ).

Figure 5 plots the limiting value of the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}$ versus the forepoling stiffness parameter ( $\alpha$ ), from Eq. (14b) by setting $\Omega \mathrm{f}=1.4$ (limiting face stability). The parameter $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}$ is the value of $\left(\Lambda_{f}\right)$ causing face extrusion $\Omega_{\mathrm{f}}=1.4$ which, by analogy to the unsupported tunnel faces (Eq. 5), corresponds to limiting unstable tunnel faces. Thus, Fig. 5 gives the values of $\left(\Lambda_{f}\right)$ where face instability occurs, with increasing stiffness of the forepoles. Stiffness values larger than $\alpha=0.20$ correspond to forepoling diameters larger than those typically used (up to about 200 mm ) and thus the achieved improvement is only theoretical. For typical diameters of the forepoling tubes ( $\mathrm{d}=60-120 \mathrm{~mm}$ ), the parameter $\alpha=0.10-0.15$ which gives $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=0.90-0.80$ (i.e., $10-20 \%$ reduction of the limiting face stability parameter with respect to the corresponding value of the unsupported face).

Using Eq. (2), and the limiting values of $\left(\Lambda_{f}\right)$ shown in Fig. 5, Eq. (15) gives the limiting value of ground strength $\left(\sigma_{\mathrm{cm}}\right)_{\text {lim }}$, which is the lowest ground strength


Fig. 4 Relationship of $\left(\Omega_{f}\right)$ versus $\left(\Lambda_{f}\right)$ for selected values of the forepoling stiffness parameter $(\alpha)$. The thick black line corresponds to the unsupported tunnel face $(\alpha=0)$. The dashed line $\left(\Omega_{\mathrm{f}}=1.4\right)$ corresponds to limiting face stability


Fig. 5 Correlation of the limiting value of the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$ versus the forepoling stiffness parameter ( $\alpha$ ). Values of $\alpha>0.20$ are not examined as they correspond to unrealistically stiff forepoling tubes ( $\mathrm{d}>200 \mathrm{~mm}$ )
to ensure limiting face stability for a given tunnel size (D), overburden depth (H) and face support with forepoling stiffness parameter ( $\alpha$ ).

$$
\begin{equation*}
\left(\sigma_{c m}\right)_{\lim }=0.263 \gamma H \sqrt{1+(2 / 3) K_{o}}\left(\frac{D}{H}\right)^{0.35}\left(\Lambda_{f}\right)_{\lim } \tag{15}
\end{equation*}
$$

Figure 6 plots the safety factor (SF) of the tunnel face (defined by Eq. 6) versus the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$, for selected values of the forepoling stiffness parameter $(\alpha)$. For each value of $(\alpha)$, the limiting parameter $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}$ is obtained from Fig. 5. The


Fig. 6 Correlation of the Safety Factor (SF) against face stability with the stability parameter $\left(\Lambda_{\mathrm{f}}\right)$ for selected values of the forepoling stiffness parameter ( $\alpha$ )
thick black line corresponds to the unsupported tunnel face, where $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=1$. For typical diameters of the forepoling tubes ( $\alpha=0.10-0.15$ ), the safety factor of the excavation face increases by $15-20 \%$.

## 5 Analysis of Face Support with Fiberglass Nails (FGN)

Figure 7a plots the calculated decrease of the face extrusion parameter ( $\Delta \Omega_{\mathrm{f}}$ ), normalized with the corresponding face extrusion of the unsupported face $\left(\Omega_{\mathrm{fo}}\right)$, versus the face stability parameter $\left(\Lambda_{f}\right)$ (defined by Eq. 2) for tunnel faces supported with three


Fig. 7 a Effect of Fiber-Glass Nail (FGN) density on the reduction of the average face extrusion, plotted versus the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$. b Effect of Fiber-Glass Nail (FGN) density on the reduction of the average face extrusion, plotted versus the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$. The vertical axis is normalized with an optimally selected FGN density parameter ( $\beta$ )
densities of Fiber-Glass nails (FGN). Nail grids of higher density reduce face extrusion more, while larger values of the face stability parameter, corresponding to better ground strength/overburden stress combinations, cause smaller face extrusions for all grid densities. For $\Lambda_{f}>2$, face extrusion is very small even in unsupported faces ( $\Omega_{\mathrm{fo}}<0.5$ ) and thus the additional decrease of face extrusion due to face reinforcement is negligible for all FG grid densities, rendering the use of FG nails as practically useless.

In Fig. 7b, the vertical axis is normalized with a FGN density parameter ( $\beta$ ), defined by Eq. (12b). Parameter ( $\beta$ ) was optimally selected to reduce the scatter of the face extrusion reductions ( $\Delta \Omega_{\mathrm{f}}$ ) in Fig. 7a. The best fit curve can be expressed by the formula (combined with Eq. 4):

$$
\begin{align*}
\left(\frac{1}{\beta}\right)\left(\frac{\Delta \Omega}{\Omega_{f o}}\right) & =0.25\left(\Lambda_{f}\right)^{-1.30} \Rightarrow \Delta \Omega_{f} \\
& =0.35 \beta\left(\Lambda_{f}\right)^{-2.5} \tag{16a}
\end{align*}
$$

Using this formula, the face extrusion parameter $\left(\Omega_{\mathrm{f}}\right)$ of the supported tunnel faces can be expressed as:

$$
\begin{align*}
\Omega_{f} & =\Omega_{f o}\left[1-0.25 \beta\left(\Lambda_{f}\right)^{-1.3}\right] \Rightarrow \Omega_{f} \\
& =1.4\left(\Lambda_{f}\right)^{-1.2}\left[1-0.25 \beta\left(\Lambda_{f}\right)^{-1.3}\right] \tag{16b}
\end{align*}
$$

Using Eq. (1), the above formula can be used to calculate the average face extrusion $\left(\mathrm{U}_{\mathrm{h}}\right)$ for various ground strength/overburden stress combinations and various FGN densities (i.e., values of the $\beta$ parameter):
$\frac{U_{h}}{D}=1.4\left(\frac{p_{o}}{E}\right)\left(\Lambda_{f}\right)^{-1.2}\left[1-0.25 \beta\left(\Lambda_{f}\right)^{-1.3}\right]$
Using Eq. (16b), Fig. 8 plots the relationship of the face extrusion parameter $\left(\Omega_{f}\right)$ versus ( $\Lambda_{f}$ ), for selected values of FGN densities ( $\beta$ ). Appreciable reduction of face extrusion occurs for $\Lambda_{f}<1$, where the unsupported face has limiting stability. For FGN density $\beta>0.675$, the tunnel face is stable for practically any ground strength/overburden stress combinations (i.e., any value of $\Lambda_{\mathrm{f}}$ ).

Figure 9 plots the limiting value of the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}$ versus the FGN density parameter $(\beta)$. The parameter $\left(\Lambda_{\mathrm{f}}\right)$ lim is the value of $\left(\Lambda_{f}\right)$ causing face extrusion $\Omega_{\mathrm{f}}=1.4$ which, by analogy to the unsupported tunnel faces (Eq. 5), corresponds to unstable tunnel faces. Thus, Fig. 9 gives the limiting values of ( $\Lambda_{\mathrm{f}}$ ) where face instability occurs, with


Fig. 8 Relationship of $\left(\Omega_{f}\right)$ versus $\left(\Lambda_{f}\right)$ for selected values of FGN density parameter ( $\beta$ ). The thick black line corresponds to the unsupported tunnel face $(\beta=0)$. The dashed line ( $\Omega_{\mathrm{f}}=1.4$ ) corresponds to limiting face stability


Fig. 9 Correlation of the limiting value of the face stability parameter $\left(\Lambda_{f}\right)$ versus the FGN density parameter ( $\beta$ )
increasing FGN density. For FGN densities $\beta>0.92$, the tunnel face is stable for practically any ground strength/overburden stress combinations (i.e., any value of $\Lambda_{f}$ ). For typical FG nail densities (one nail per $12.5 \div 4 \mathrm{~m}^{2}$ of tunnel face), the FG density parameter $\beta=0.50-0.74$, which gives $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim- }}$ $=0.80-0.50$ (i.e., $20-50 \%$ reduction with respect to the unsupported face). Comparing these reductions with those of face support by forepoling tubes ( $10-20 \%$ reduction with respect to the unsupported face), it is concluded that the lightest FG nail density ( 1 nail per $12.5 \mathrm{~m}^{2}$ of face area) achieves the same improvement of face stability as the heaviest
forepoling tubes (diameter about 200 mm ), giving a clear advantage to face support by FG nails.

Using Eq. (2), and the limiting values of $\left(\Lambda_{f}\right)$ shown in Fig. 9, Eq. (17) gives the limiting value of ground strength $\left(\sigma_{\mathrm{cm}}\right)_{\text {lim }}$, which is the lowest ground strength to ensure limiting face stability for a given tunnel size (D), overburden depth $(\mathrm{H})$ and face support with FGN density parameter ( $\alpha$ ).

$$
\begin{equation*}
\left(\sigma_{c m}\right)_{\lim }=0.263 \gamma H \sqrt{1+(2 / 3) K_{o}}\left(\frac{D}{H}\right)^{0.35}\left(\Lambda_{f}\right)_{\lim } \tag{17}
\end{equation*}
$$

Figure 10 plots the safety factor (SF) of the tunnel face (defined by Eq. 6) versus the face stability parameter ( $\Lambda_{\mathrm{f}}$ ), for selected values of the FGN density parameter $(\beta)$. The thick black line corresponds to the unsupported tunnel face (where $\mathrm{SF}=1$ for $\Lambda_{\mathrm{f}}=1$ ). For FGN densities $\beta>0.92$, the tunnel face is stable (SF $>1$ ) for practically any value of $\Lambda_{\mathrm{f}}$.

## 6 Other Results for Supported Tunnel Faces

By analogy to the unsupported tunnel faces (Eqs. 8, 9, 10) the following equations give the the radial displacement $\left(U_{R}\right)$ of the tunnel wall, the volume loss (VL) and the deconfinement ratio $(\lambda)$ at the excavation face, for tunnels with supported faces, in terms of the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)$ and the corresponding


Fig. 10 Correlation of the Safety Factor (SF) against face stability with the stability parameter $\left(\Lambda_{\mathrm{f}}\right)$ for selected values of the FGN density parameter ( $\beta$ )
limiting value $\left(\Lambda_{\mathrm{f}}\right)_{\mathrm{lim}}$ which depends on the type and capacity of the face support (Fig. 5 for forepoles and Fig. 9 for FG nails):

$$
\begin{align*}
& \frac{U_{R}}{D}=1.75\left(\frac{p_{o}}{E}\right)\left(\frac{\Lambda_{f}}{\left(\Lambda_{f}\right)_{\lim }}\right)^{-1.2}  \tag{18}\\
& V L=1.83\left(\frac{p_{o}}{E}\right)\left(\frac{\Lambda_{f}}{\left(\Lambda_{f}\right)_{\lim }}\right)^{-1.2}  \tag{19}\\
& \lambda=0.25+0.75 \exp \left(-\frac{1}{2} \frac{\Lambda_{f}}{\left(\Lambda_{f}\right)_{\lim }}\right) \tag{20}
\end{align*}
$$

## 7 Application Example

The above formulae, produced by normalizing the results of many parametric finite element analyses of tunnel faces supported with forepoling or FG nails, can assist in the selection of suitable face support measures in unstable or marginally stable tunnel faces. Some typical examples are given below, with the objective to compare the effectiveness of forepoling versus FG nails in improving face stability.

A tunnel with width $\mathrm{D}=10 \mathrm{~m}$ and section area $\mathrm{A}=67.3 \mathrm{~m}^{2}$ is excavated at depth $\mathrm{H}=250 \mathrm{~m}$ in a heavily fractured rockmass, with intact strength $\sigma_{\mathrm{ci}}$ $=10 \mathrm{MPa}$, intact modulus $\mathrm{Ei}=2.5 \mathrm{GPa}$ and $\mathrm{GSI}=$ 25. The ground has unit weight $\gamma=23 \mathrm{kN} / \mathrm{m}^{3} \mathrm{\kappa} \alpha \mathrm{l}$ $\mathrm{K}_{\mathrm{o}}=0.6$.

The calculated rockmass strength and modulus are (Eqs. 3 b and 3 c ): $\sigma_{\mathrm{cm}}=533 \mathrm{kPa}, \mathrm{E}=150 \mathrm{MPa}$, $\mathrm{p}_{\mathrm{o}}=4600 \mathrm{kPa}$ and $\left(\mathrm{p}_{\mathrm{o}} / \mathrm{E}\right)=4.6 / 150=0.0307$. The face stability parameter is (Eq. 2): $\Lambda_{f}=0.92<1$, indicating that the unsupported tunnel face is unstable, with safety factor (Eq. 6 or 7 ): $\mathrm{SF}_{\mathrm{o}}=0.92$.

For the unsupported tunnel face, the radial displacement $\left(\mathrm{U}_{\mathrm{R}}\right)$ of the tunnel wall at the excavation face is (Eq. 8): $U_{R} / D=6 \%$, the volume loss is (Eq. 9): $\mathrm{VL}=6.2 \%$ and the deconfinement ratio at the tunnel face is (Eq. 10): $\lambda=0.724$.

If the tunnel face is supported with heavy forepoling tubes of diameter $114 / 100 \mathrm{~mm}$, spaced every 50 cm on a top arch of 120 degrees ( 22 tubes in total), the forepoling stiffness parameter is (Eq. 12a): $\alpha=0.151$ which corresponds to a limiting value of the face stability parameter (Fig. 5) $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=0.821$
and the safety factor of the tunnel face is (Eq. 6): $\mathrm{SF}=0.919 / 0.821=1.12>1$ (stable face). For this configuration, the radial displacement ( $\mathrm{U}_{\mathrm{R}}$ ) of the tunnel wall at the excavation face is (Eq. 18): $\mathrm{U}_{\mathrm{R}} /$ $\mathrm{D}=4.7 \%$, the volume loss is (Eq. 19): $\mathrm{VL}=4.9 \%$ and the deconfinement ratio at the tunnel face is (Eq. 20): $\lambda=0.679$. These values are a little lower than the corresponding values of the unsupported tunnel face, showing that forepoling has some effect in improving face stability conditions.

If the tunnel face is supported with very heavy forepoling tubes of diameter $168 / 154 \mathrm{~mm}$, spaced every 50 cm on a top arch of 120 degrees (again 22 tubes in total), the forepoling stiffness parameter is $\alpha=0.176$ which which corresponds to a limiting value of the face stability parameter $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=0.761$ and the safety factor of the tunnel face is $\mathrm{SF}=1.21$ $>1$. This is the largest possible safety factor, since the heaviest possible forepoling was used. For this configuration, the radial displacement $\left(\mathrm{U}_{\mathrm{R}}\right)$ of the tunnel wall at the excavation face is $U_{R} / D=4.3 \%$, the volume loss is $\mathrm{VL}=4.5 \%$ and the deconfinement ratio at the tunnel face is $\lambda=0.66$. These values are very little lower than those corresponding to the $114 / 100 \mathrm{~mm}$ forepoling, indicating that even very heavy forepoling does not increase the safety factor of the tunnel face significantly $\left(\mathrm{SF}_{\mathrm{o}}=0.92\right.$ of the unsupported face, increased to $\mathrm{SF}=1.21$ for the most heavy forepoling).

Alternatively, if the tunnel face is supported with only $\mathrm{n}=8 \mathrm{FG}$ nails ( 1 nail every $8.5 \mathrm{~m}^{2}$ of face area, $\mathrm{Pu}=200 \mathrm{kN}$ and $\mathrm{F}=2$ ), the FG density parameter is (Eq. 12b): $\beta=0.569$, which gives limiting value of the face stability parameter (Fig. 9) $\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=0.75$ and the safety factor of the tunnel face is (Eq. 6): $\mathrm{SF}=0.919 / 0.75=1.22>1$. For this configuration, the radial displacement $\left(\mathrm{U}_{\mathrm{R}}\right)$ of the tunnel wall at the excavation face is (Eq. 18): $\mathrm{U}_{\mathrm{R}} / \mathrm{D}=4.2 \%$, the volume loss is (Eq. 19): VL $=4.4 \%$ and the deconfinement ratio at the tunnel face is (Eq. 20): $\lambda=0.657$. These face parameters, achieved with only 8 FG nails, are similar to the result achieved with the heaviest possible forepoling ( 22 tubes of $168 / 154 \mathrm{~mm}$ ). Obviously, the cost of the FG nails is much lower than the corresponding cost of the forepoling.

If the tunnel face is supported with $\mathrm{n}=14 \mathrm{FG}$ nails (1 nail every $4.8 \mathrm{~m}^{2}$ of face area, $\mathrm{Pu}=200 \mathrm{kN}$ and $\mathrm{F}=2$ ), the FG density parameter is $\beta=0.693$, which gives limiting value of the face stability parameter
$\left(\Lambda_{\mathrm{f}}\right)_{\text {lim }}=0.61$ and the safety factor of the tunnel face is $\mathrm{SF}=0.919 / 0.61=1.51$. For this configuration, the radial displacement $\left(U_{R}\right)$ of the tunnel wall at the excavation face is $U_{R} / D=3.3 \%$, the volume loss is $\mathrm{VL}=3.4 \%$ and the deconfinement ratio at the tunnel face is $\lambda=0.60$. These face parameters, achieved with 14 FG nails, are much better than the result achieved with the heaviest possible forepoling ( 22 tubes of $168 / 154 \mathrm{~mm}$ ), where the safety factor is only $\mathrm{SF}=$ 1.21 at a much larger cost.

The difference in effectiveness of the FG nails is even larger in weak ground, where even the heaviest forepoling cannot achieve face stability. For example, in a tunnel excavated in heavily fractured rockmass with intact strength $\sigma_{\mathrm{ci}}=8 \mathrm{MPa}$, intact modulus $\mathrm{Ei}=2 \mathrm{GPa}, \mathrm{GSI}=20$ at depth $\mathrm{H}=180 \mathrm{~m}$, the safety factor of the unsupported face is: $\mathrm{SF}_{\mathrm{o}}=0.75$ (unstable face). With the most heavy forepoling (168/ 154 mm spaced at 50 cm ), the safety factor increases to $\mathrm{SF}=0.98$ and the face is still marginally stable. If the tunnel face is supported with FG nails, the same improvement ( $\mathrm{SF}=0.98$ ) can be achieved with only 8 FG nails (one nail every $8.5 \mathrm{~m}^{2}$ of tunnel face). With 13 nails (one nail every $5.2 \mathrm{~m}^{2}$ of tunnel face) the safety factor is increased to $\mathrm{SF}=1.21$ and with 22 nails (one nail every $3 \mathrm{~m}^{2}$ of tunnel face) the safety factor is increased to $\mathrm{SF}=1.97$. In the last case, the radial displacement $\left(\mathrm{U}_{\mathrm{R}}\right)$ of the tunnel wall at the excavation face is $U_{R} / D=2.8 \%$, the volume loss is $\mathrm{VL}=2.9 \%$ and the deconfinement ratio at the tunnel face is $\lambda=0.53$. The advantage of FG nails in improving face stability in very poor rockmasses, compared to the use of forepoling umbrellas, is evident.

## 8 Conclusions

Georgiou et al (2021) have investigated stability of unsupported tunnel faces by parametric 3D finite element analyses using the Finite Element (FE) Code Simulia Abaqus. The present study extends these methods to include tunnel faces supported with forepoling umbrellas (FPU) and fiber-glass nails (FGN). In each case of ground conditions and overburden depth, a number of FE analyses are performed using various densities of FGN reinforcement or forepoling umbrellas to calculate the average face extrusion, which is obviously lower than that of
the corresponding unsupported face. The analyses use the average face extrusion as a measure of face stability, considering that face instability is associated with large face extrusions while the safety factor against face instability can be correlated with lower face extrusions in case of pre-supported tunnel faces. The results of the analyses are normalized and a set of semi-empirical formulae and design graphs are produced to calculate the safety factor of supported tunnel faces against instability and other useful quantities in tunnel design (average face extrusion, volume loss and deconfinement coefficient) as a function of ground strength, overburden depth and amount of face reinforcement.

The analyses show that tunnel face reinforcement with FG nails is much more effective and less costly in securing face stability than the use of forepoling umbrellas. It is shown that even a coarse grid of FG nails can achieve better results than very heavy forepoling, and the difference in effectiveness is more pronounced in weaker ground and or deeper tunnels.

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