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# ΣΚΕΨΕΙΣ ΓΙΑ ΤΑ ΜΑΘΗΜΑΤΙΚΑ

## Η Φιλοσοφία των Μαθηματικών

Thinking about mathematics: The philosophy of mathematics. ΣΚΕΨΕΙΣ ΓΙΑ ΤΑ ΜΑΘΗΜΑΤΙΚΑ: Η ΦΙΛΟΣΟΦΙΑ ΤΩΝ ΜΑΘΗΜΑΤΙΚΩΝ. Thinking about mathematics: The philosophy of mathematics. ΣΚΕΨΕΙΣ ΓΙΑ ΤΑ ΜΑΘΗΜΑΤΙΚΑ: Η ΦΙΛΟΣΟΦΙΑ ΤΩΝ ΜΑΘΗΜΑΤΙΚΩΝ. Thinking about mathematics: The philosophy of mathematics. ΣΚΕΨΕΙΣ ΓΙΑ ΤΑ ΜΑΘΗΜΑΤΙΚΑ: Η ΦΙΛΟΣΟΦΙΑ ΤΩΝ ΜΑΘΗΜΑΤΙΚΩΝ.

Μετάφραση

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